

#1a

$$\begin{aligned} & (a+b)^2 \\ &= (a+b)(a+b) \\ &= a^2 + ab + ab + b^2 \\ &= a^2 + 2ab + b^2 \end{aligned}$$

$$\begin{aligned} & a^2 + 2ab + b^2 \\ &= 2ab + a^2 + b^2 \quad \text{Re-arrange.} \\ &= 2(6) + 24 \quad \text{Substitute known values.} \\ &= 12 + 24 \\ &= 36 \quad \therefore (a+b)^2 = 36 \end{aligned}$$

#1b

$$\begin{aligned} & (x+y)^2 = 13 \\ & x^2 + 2xy + y^2 = 13 \\ & x^2 + y^2 + 2xy = 13 \\ & 7 + 2xy = 13 \\ & 2xy = 13 - 7 \\ & 2xy = 6 \\ & xy = 3 \end{aligned}$$

Expand.

Re-arrange.

Substitute known value.

$$\therefore xy = 3$$

(more on next page.)

#1c

$$(j+k)^2 = j^2 + 2jk + k^2$$

$$(j+k)^2 = j^2 + 2jk + k^2$$

Re-write as equation.

$$(6)^2 = j^2 + k^2 + 2jk$$

$$(6)^2 = 52 + 2jk$$

$$36 - 52 = 2jk$$

$$-16 = 2jk$$

$$-8 = jk$$

$$\therefore jk = -8$$

Substitute known values

#1d

$$(m+n)^2$$

$$\underline{\text{part 1}} = m^2 + 2mn + n^2$$

$$= m^2 + n^2 + 2mn$$

$$= 12 + 2mn$$

Make an expression that gets us $m^2 + n^2$

Substitute known value.

$$\underline{\text{part 2}} (m^2 + n^2)^2$$

$$= (m^2 + n^2)(m^2 + n^2)$$

$$= m^4 + m^2 n^2 + m^2 n^2 + n^4$$

$$= m^4 + 2m^2 n^2 + n^4$$

$$= m^4 + n^4 + 2m^2 n^2$$

$$= 136 + 2m^2 n^2$$

Make an expression to get $m^4 + n^4$ Substitute known values
(continued next page)

$$\underline{\text{Part 3}} \quad (m^2 + n^2)^2 \\ = (12)^2 \\ = 144$$

Back to this...
trying to set up
an equation.

Substitute
known value.

$$\underline{\text{Part 4}} \quad (m^2 + n^2)^2 = (m^2 + n^2)^2 \\ 136 + 2m^2 n^2 = 144 \\ 2m^2 n^2 = 144 - 136 \\ 2m^2 n^2 = 8 \\ m^2 n^2 = 4$$

Now we have
an equation!

Hmm... getting close.

$$\underline{\text{Part 5}} \quad (mn)^2 = m^2 n^2$$

Make an equation
that gets us
 $m^2 n^2$.

$$(mn)^2 = 4$$

$$\sqrt{(mn)^2} = \sqrt{4}$$

$$\therefore mn = 2$$

$$\text{or } mn = -2 \quad \therefore (2)^2 = 4$$

$$\text{and } (-2)^2 = 4$$

Substitute.

IMPORTANT NOTE : part 1 didn't end up
being useful. That's OK!

WDYDWYDKWTD

Try something and see
where it leads!